## MathExcel Worksheet B #2: Partial Fractions and Numerical Integration

1. Evaluate the following indefinite integrals.

(a) 
$$\int \frac{e^x}{e^{2x} + 3e^x + 2} dx$$
  
(b)  $\int \frac{x^3 - 4x + 1}{x^2 - 3x + 2} dx$ 

(c) 
$$\int \frac{y}{(y+4)(2y-1)} \, dy$$

2. Evaluate

$$\int \frac{1}{x^2 + k} \, dx$$

where k is a constant. If you aren't sure where to start, try evaluating the integral for a specific value of k.

- 3. Consider the integral:  $\int_{-1}^{1} \ln(1+x^2) dx$ 
  - (a) Use the trapezoid rule with n = 4 to approximate the integral.
  - (b) Use Simpson's rule with n = 6 to approximate the integral.
  - (c) How many subintervals would you use in order to approximate the integral with the Midpoint rule?

4. Consider the integral 
$$\int_0^2 \sqrt{x} \, dx$$
.

- (a) Evaluate the integral exactly.
- (b) What is the largest error you would expect from an approximation using the trapezoid rule? Using Simpson's rule?
- (c) Use the trapezoid rule with n = 6 to approximate the integral. Is this an overestimate or underestimate? Calculate the error.
- (d) Use Simpson's rule with n = 6 to approximate the integral. Calculate the error.
- (e) How many subintervals (i.e. what value of n) are needed to guarantee a Midpoint approximated within 0.0001 of the exact value?
- 5. Numerical integration allows us to approximate irrational numbers. Consider the integral  $\int_0^1 \frac{4}{1+x^2} dx$ .
  - (a) What is the exact value of the integral?
  - (b) Use Simpson's rule to approximate the value within 0.0001.
- 6. For each of the following integrals, decide which is improper. For the improper integrals, set up BUT DO NOT EVALUATE the corresponding limit problem.

(a) 
$$\int_{-\infty}^{3} x^2 dx$$
 (c)  $\int_{0}^{1} \frac{x}{x^2 + 3} dx$   
(b)  $\int_{-\infty}^{\infty} \frac{1}{1 + x^2} dx$  (d)  $\int_{\frac{\pi}{3}}^{\frac{2\pi}{3}} \tan \theta d\theta$ 

(e) 
$$\int_{-2}^{2} \frac{t}{\sqrt{9-t^{2}}} dt$$
  
(f)  $\int_{0}^{10000} \ln(x^{2}+1) dx$ 

(g) 
$$\int_{-\infty}^{\infty} \frac{1}{s^2 + 2s - 15} ds$$
  
(h)  $\int_{-1}^{1} \frac{\sin y}{\sqrt{y^2 - y}} dy$